

A Survey – Methods of Missing Data Imputation

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ABSTRACT- Missing values in attributes. Several schemes have been studied to overcome the drawbacks produced by missing values in data mining tasks; one of the most well known is based on preprocessing, formerly known as imputation. This paper reviews methods for handling missing data in a research study.

1. Introduction

Missing data is a problem because nearly all standard statistical methods presume complete information for all the variables included in the analysis. A relatively few absent observations on some variables can dramatically shrink the sample size. As a result, the precision of confidence intervals is harmed, statistical power weakens and the parameter estimates may be biased. Appropriately dealing with missing can be challenging as it requires a careful examination of the data to identify the type and pattern of missingness, and also a clear understanding of how the different imputation methods work. Sooner or later all researchers carrying out empirical research will have to decide how to treat missing data. In a survey, respondents may be unwilling to reveal some private information, a question may be inapplicable or the study participant simply may have forgotten to answer it. Accordingly, the purpose of this report is to clearly present the

essential concepts and methods necessary to successfully deal with missing data.

2. Missing data mechanisms

There are different assumptions about missing data mechanisms:

- a) Missing completely at random (MCAR): Suppose variable Y has some missing values. We will say that these values are MCAR if the probability of missing data on Y is unrelated to the value of Y itself or to the values of any other variable in the data set. However, it does allow for the possibility that “missingness” on Y is related to the “missingness” on some other variable X. (Briggs et al., 2003) (Allison, 2001)
- b) Missing at random (MAR)-a weaker assumption than MCAR-

The probability of missing data on Y is unrelated to the value of Y after controlling for other variables in the analysis (say X). Formally: $P(Y \text{ missing} | Y, X) = P(Y \text{ missing} | X)$ (Allison, 2001). c) Not missing at random (NMAR): Missing values do depend on unobserved values.

3. Literature Review

We can find more recent analysis and proposals of imputation methods, which considers an increasing number of techniques compared:

- Hruschka et al. [28] propose two imputation methods based on Bayesian networks. They



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compare them with 4 classical imputation methods: EM, Data Augmentation, C4.5, and the CMC method, using 4 nominal data sets from the UCI repository [3] with natural MVs (but inducing MVs in them as well). In their analysis, they employ 4 classifiers as follows: one-rule, Naïve-Bayes, C4.5, and PART. As performance measures, the authors measure the prediction value (i.e., the similarity of the imputed value to the original removed one) and the classification accuracy obtained with the four mentioned models. From the results, the authors state that better prediction results do not imply better classification results.

- Farhangfar et al. [18] take as the objective of their paper to develop a unified framework supporting a host of imputation methods. Their study inserts some imputation methods into their framework (Naïve-Bayes and Hot Deck) and compares this with other basic methods: mean, Linear Discriminant Analysis, Logreg, etc. All their experimentation is based on discrete data, so they use the “accuracy” of imputed values against randomly generated MVs. The relation of this imputation accuracy to classification accuracy is not studied. In Farhangfar et al. [19], the previous study is extended using discrete data, comparing with more classical imputation methods. This study uses a representative method of several classifiers’ types as follows: decision trees, instance-based learning, rule-based classifier, probabilistic methods, and SVMs by means of boosting [51]. The MVs are produced artificially in a wide-ranging amount for each of the data sets, and the results obtained from the classification of imputed data are compared with the ones with MVs. This study shows that the impact of the imputation

varies among different classifiers and that imputation is beneficial for most amounts of MVs above 5% and that the amount of improvement does not depend on the amount of MVs. The performed experimental study also shows that there is no universally best imputation method.

- Song et al. [56] study the relationship between the use of the KNNI method and the C4.5 performance (counting with its proper MV technique) over 6 data sets of software projects. They emphasize the different MVs’ mechanisms (MCAR, MAR, and NMAR) and the amount of MVs introduced. From their analysis, they found results that agree with Batista and Monard [6]: KNNI can improve the C4.5 accuracy. They ran a Mann–Whitney statistical test to obtain significant differences in this statement. They also show that the missingness mechanism and pattern affect the classifier and imputation method performance.

- Twala [58] empirically analyzes 7 different procedures to treat artificial MVs for decision trees over 21 real data sets. From the study, it can be concluded that listwise deletion is the worst choice, while the multiple imputation strategy performs better than the rest of the imputation methods (particularly those with high amounts of MVs), although there is no outstanding procedure.

- García-Laencina et al. [23] evaluate the influence of imputing MVs into the classification accuracy obtained by an artificial neural network (multilayer perceptron). Four imputation techniques are considered as follows: KNNI, SOM imputation, MLP imputation, and EM over one synthetic and two real data sets, varying the amount of MVs introduced. They conclude that in real-life scenarios a detailed study is required in order to

evaluate which MVs estimation can help to enhance the classification accuracy.

- Luengo et al. [35] study several imputation methods for RBFNs classifiers, both for natural and artificial (MCAR) MVs. From their results can be seen that the EC method has a good synergy with respect to the RBFN methods, as it provides better improvements in classification accuracy.
- Ding and Simonoff [14] investigate eight different missingness patterns, depending on the relationship between the missingness and three types of variables, the observed predictors, the unobserved predictors (the missing values), and the response variable. They focus on the case of classification trees for binary data (C4.5 and CART) using a modeling bankruptcy database, showing that the relationship between the missingness and the dependent variable, as well as the existence or non-existence of MVs in the testing data, is the most helpful criterion to distinguish different MVs methods.
- Gheyas and Smith [25] propose a single imputation method and a multiple imputation method, both of them based on a generalized regression neural network (GRNN). Their proposal is compared with 25 imputation methods of different natures, from machine learning methods to several variants of GRNNs. Ninety-eight data sets are used in order to introduce MVs with MCAR, MAR, and NMAR mechanisms. Then, the results of the imputation methods are compared by means of 3 different criteria, using the following three classifiers: MLP, logistic regression, and a GRNN-based classifier, showing the advantages of the proposal.

Recently, the treatment of MVs has been considered in conjunction with other hot topics in classification, like imbalanced data sets, semi-supervised learning, temporal databases, scalability, and the presence of noisy data. Nogueira et al. [41] presented a comparison of techniques used to recover values in a real imbalanced database, with a massive occurrence of MVs. This makes the process of obtaining a set of representative records, used for the recovering techniques, difficult. They used C4.5, Naïve-Bayes, K-NN, and multilayer perceptron as classifiers. To treat the MVs, they applied several techniques as follows: default value substitution or related attribute recovery. The latter tries to obtain the missing value from the information of another attribute. In addition to this, cleaning of instances/attributes with too many MVs was also carried out.

Saar-Tsechansky and Provost [52] compare several different methods (predictive value imputation, the distribution-based imputation used by C4.5 and using reduced models) for applying classification trees to instances with missing values. They distinguish between MVs in “training” (usual MVs) and MVs in “prediction” time (i.e., test partition) and adapt the novel-reduced models to this scenario. The results show that for the predictive value imputation and C4.5 distribution based, both can be preferable under different conditions. Their novel technique (reduced models) consistently outperforms the other two methods based on their experimentation.

Matsubara et al. [36] present an adaptation of a semi-supervised learning algorithm for imputation. They impute the MV using the C4.5 and Naïve-



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Bayes classifiers by means of a ranking aggregation to select the best examples. They compare the method with three qualitative UCI [3] data sets applying artificial MVs and perform a similar study to the one presented by Batista and Monard [6], comparing with the KNNI and MC methods. Using a non-parametric statistical test, they demonstrate the better performance of the new method over the other two in some cases.

Merlin et al. [38] propose a new method for the determination of MVs in temporal databases based on self-organizing maps. Using two classifiers for the spatial and tempo- ral dependencies, improvements in respect of the EM method in a hedge fund problem

Conclusion

Our main objective was comparison of the methods to deal with missing data imputation. These methods are promising for the best performances. However it is risky for us to conclude that they are the best methods among all other methods . Our future work is to conclude a best method to find missing data.

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